

# GCSE

## **Mathematics**

Foundation Tier Unit 1 Statistics and Number Mark scheme

43601F

November 2015

Version 1.0 Final.

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aga.org.uk

### **Glossary for Mark Schemes**

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

| M               | Method marks are awarded for a correct method which could lead to a correct answer.  |
|-----------------|--|
| Α               | Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied. |
| В               | Marks awarded independent of method.   |
| ft              | Follow through marks. Marks awarded for correct working following a mistake in an earlier step.  |
| SC              | Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.                        |
| M dep           | A method mark dependent on a previous method mark being awarded.   |
| B dep           | A mark that can only be awarded if a previous independent mark has been awarded.   |
| oe              | Or equivalent. Accept answers that are equivalent.   |
|                 | eg, accept 0.5 as well as $\frac{1}{2}$  |
| [a, b]          | Accept values between a and b inclusive.   |
| 3.14            | Accept answers which begin 3.14 eg 3.14, 3.142, 3.149.   |
| Use of brackets | It is not necessary to see the bracketed work to award the marks.  |

Examiners should consistently apply the following principles

#### **Diagrams**

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

#### Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

#### Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

#### Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

#### Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

#### **Further work**

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

#### Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

#### Work not replaced

Erased or crossed out work that is still legible should be marked.

#### Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

#### **Premature approximation**

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

| Q    | Answer  | Mark        | Comments  |  |
|------|---|-------------|---|--|
| 1(a) | 24  | B1          | Accept [23.5, 24.5] Ignore any words eg May                         |  |
|      | Bar of height 25                                  | B1          | $\pm \frac{1}{2}$ small square                                      |  |
|      | Ad  | lditional g | guidance  |  |
| 1(b) | Mark the intention                                |             |   |  |
|      | Condone freehand                                  |             |   |  |
|      | Ignore shading or lack of shading                 |             |   |  |
|      | June and September                                | B2          | B1 one correct month and no more than one incorrect month           |  |
| 1(c) |   |             |   |  |
|      |   |             |   |  |
| 1(d) | [24, 31.5] – 19 or (July =) 31                    | M1          |   |  |
| I(u) | 12  | A1          |   |  |
|      | 25 × 14   | M1          |   |  |
| 2(a) | 350 or 3.5(0)                                     | A1          | 650 or 6.5 or 6.50p implies M1A1                                    |  |
| 2(a) | 6.50  | Q1ft        | Strand (i) Correct money notation ft 10 – their 3.5(0) if M1 scored |  |
|      | <u> </u>  |             |   |  |
| 2(b) | $\frac{14}{50}$ or $\frac{7}{25}$ or 0.28 or 28%  | B1          | oe<br>Ignore words eg unlikely                                      |  |
|      | 1   |             |   |  |
| 2(5) | 36 or 18 or 0.72 or 72%                           | B1ft        | 0e ft their part (b)  |  |
| 2(c) | $\frac{36}{50}$ or $\frac{18}{25}$ or 0.72 or 72% |             | ft their part (b) Ignore words eg likely                            |  |

| Q | Answer   | Mark       | Comments   |  |
|---|--|------------|--|--|
|   |  |            |  |  |
| 3 | Correct numbers of circles in each row   | B2         | B1 for two or more rows correct Accept any orientation for the half-circles  |  |
|   | Appropriate alignment of symbols   | Q1ft       | Strand(ii) Organise their work clearly ft their symbols All four rows must be attempted with at least one half-circle used |  |
|   | Ad   | ditional g | uidance  |  |
|   | Ignore any variation of symbol size  |            |  |  |
|   | For Q1 the lengths of each row must be, in descending order; 1 <sup>st</sup> , 5 <sup>th</sup> , 4 <sup>th</sup> , 3 <sup>rd</sup> , 2 <sup>nd</sup> |            |  |  |

| Q    | Answer   | Mark  | Comments  |  |  |
|------|--|-------|---|--|--|
|      | 17.31 or Medium chosen   | B1    | May be implied                                      |  |  |
|      | their 17.31 + 7.5 or 24.81 or their 17.31 $\times$ 7 or 121.17 or their 7.5 $\times$ 7 or 52.5 | M1    |   |  |  |
| 4    | their 24.81 $\times$ 7 (+ 39.6) or their 17.31 $\times$ 7 + 7.5 $\times$ 7 (+ 39.6) or 173.67  | M1dep |   |  |  |
|      | 213.27   | A1    | SC3 209.07 or 290.55<br>Condone £213.27p            |  |  |
|      | Additional guidance  |       |   |  |  |
|      | Adding 39.6 $\times$ 7 scores a maximum of B1 M1 M0 A0   |       |   |  |  |
| 5(a) | 25%  | B1    |   |  |  |
| 5(b) | (360 – ) 90 + 81 + 42 + 33 + 87<br>or<br>333   | M1    | Allow one error or omission or extra                |  |  |
|      | 27   | A1    |   |  |  |
|      |  |       | 81 . 42   |  |  |
| 5(c) | 81 : 42  | M1    | oe eg $\frac{31}{360}$ : $\frac{42}{360}$           |  |  |
|      | 27 : 14  | A1    | SC1 correct simplification of their ratio SC1 14:27 |  |  |

| Q    | Answe  | r       | Mark     | Comments   |       |
|------|--|---------|----------|--|-------|
| 6(a) | mode   |         | B1       |  |       |
| 6(b) | 163  |         | B1       |  |       |
|      | Selects 205 or 153                                 |         | M1       |  |       |
| 6(c) | 52   |         | A1       | SC1 answer of 48 or 31   |       |
|      |  |         |          |  |       |
|      | 9 brown-eyed boys <b>and</b><br>9 brown-eyed girls | d       | B1       |  |       |
|      | 17 boys <b>and</b> 23 girls                        |         | B1       |  |       |
|      | 12 blue-eyed girls <b>and</b> 5 green-eyed boys    |         | B1ft     | ft their 17 – their 9 – 3<br><b>and</b> their 23 – their 9 – 2   |       |
|      | 15 blue eyes <b>and</b> 7 green e                  | en eyes | B1ft     | ft 3 + their 12 <b>and</b> their 5 + 2 if their column totals 40 | third |
| 7(a) | The correct table is                               |         | <u>'</u> |  |       |
|      |  | Boys    | Girls    | Total  |       |
|      | Brown  | 9       | 9        | 18   |       |
|      | Blue   | 3       | 12       | 15   |       |
|      | Green  | 5       | 2        | 7  |       |
|      | Total  | 17      | 23       | 40   |       |
|      |  |         |          |  |       |
|      | 18 ÷ 40 (× 100)                                    |         | M1       |  |       |
| 7(b) | 45   |         | A1       |  |       |

| Q    | Answer   | Mark        | Comments  |             |
|------|--|-------------|---|-------------|
| 8(a) | $\frac{1}{6}$ (× 420) or $\frac{70}{420}$ seen   | M1          | ое  |             |
| July | 70   | A1          | Accept 70 out of 420  |             |
| 8(b) | $\frac{23}{50}$ and 0.46 and 46%   | B2          | B1 circles one or two correct values no more than one incorrect values              |             |
| 9(a) | 7 + 10 + 4 + 3 (= 24)  | B1          | If the only working is in the table tand 24 must be shown                           | he addition |
|      | $7 \times 1$ or $10 \times 2$ or $20$ or $4 \times 3$ or $3 \times 4$ or $12$ or $51$          | M1          | Attempt at fx   |             |
|      | $(7 \times 1 + 10 \times 2 + 4 \times 3 + 3 \times 4) \div 24$<br>or<br>their 51 ÷ 24          | M1dep       | Accept one error or missing product Condone missing brackets eg 39.5                |             |
| 9(b) | 2.125  | A1          | Accept 2 or 2.1 or 2.12 or 2.13 with fully correct working                          |             |
|      | Additional guidance  |             |   |             |
|      | One error could be an incorrect product  |             |   |             |
|      | Evidence of a correct method may be se   | en in or ar | ound the table  |             |
|      | Accept an incorrectly rounded answer if 2.125 shown M1 M1                                      |             |   | M1 M1 A1    |
|      | 2.2 × (24 × 4) or 55   | N 4 4       |   |             |
|      | 2.2 × (24 + 1) or 55   | M1          | ft FF their F4  |             |
| 9(c) | 4  | A1ft        | ft 55 – their 51  Condone an answer of 5 from a r  2.24 or an answer of 3 from a me |             |
|      | Additional guidance  |             |   |             |
|      | If using trial and improvement, must reach 55 as their final trial or clearly show it selected |             |   |             |

| Q     | Answer   | Mark      | Comments   |          |  |
|-------|--|-----------|--|----------|--|
| 10    | States a valid reason about increasing sample size or interviewing a variety of people       | B1        | eg ask more people<br>ask boys and girls<br>ask adults too |          |  |
| 11(a) | Negative B1 Accept eg strong negative, wea   |           | Accept eg strong negative, weak i                          | negative |  |
|       | One straight line through both gates (20, 75 – 90) and (80, 30 – 40)                         | B1        |  |          |  |
|       | Ac   | dditional | guidance   |          |  |
| 44(b) | Ignore outside gates   |           |  |          |  |
| 11(b) | Line must cross at least 5 large squares   |           |  |          |  |
|       | Joining points only  |           |  |          |  |
|       | If the points are joined and a line of best fit is also drawn then mark the line of best fit |           |  |          |  |
|       |  |           | ft their line of best fit $\pm \frac{1}{2}$ small square   |          |  |
| 11(c) | 66   | B1ft      | Accept any value in the range [62 awarded in (b)           |          |  |
|       |  |           |  |          |  |
|       | $\frac{1}{4}$ × 20 or 5 or 6 seen  | M1        | May be implied by $\frac{5}{20}$ or $\frac{6}{20}$         |          |  |
| 12    | $\frac{6}{21}$ or $\frac{2}{7}$  | A1        | oe<br>Accept 0.29 or 29% (or better)                       |          |  |
|       | Additional guidance  |           |  |          |  |
|       | Decimal answer is 0.285714   |           |  |          |  |

| Q                         | Answer   | Mark        | Comments  |               |
|---------------------------|--|-------------|---|---------------|
|                           | T  |             | T   |               |
|                           | $3 \times 6$ or (total = ) 18  | M1          | Implied by three integers with a s  | um of 18      |
|                           | 1, 1, 16   | A1          | May be implied by an answer of 1  | 15            |
|                           | 15   | A1ft        | ft correct calculation of the range of a group of three integers with a sum of 1. |               |
|                           | Additional guidance  |             |   |               |
|                           | The 'three integers' must be clearly in a                                    | group of th | nree  |               |
| 13                        | If more than one group of 'three integers' is given but all have a sum of 18 |             |   |               |
|                           | 0, 0, 18 with no or incorrect range given                                    |             |   | M1 A0 A0      |
| 0, 0, 18 with answer = 18 |  |             | M1 A0<br>A1ft   |               |
| 1, 3, 15 with answer = 14 |  |             |   | M0 A0 A0      |
|                           | 1, 2, 15 with answer = 14  |             |   | M1 A0<br>A1ft |
|                           | 1, 1, 16 with answer = 14  |             |   | M1 A1 A0      |

| Q  | Answer  | Mark | Comments   |  |  |
|----|---|------|--|--|--|
|    | Alternative method 1  |      |  |  |  |
|    | Correct conversion of one value to another form $\frac{5}{12}$ oe fraction or 2:3 oe ratio 41.()% or 42% or 40% 0.41() or 0.42 or 0.4   | M1   | Accept in words eg 5 out of 12 Accept missing percentage signs |  |  |
| 14 | Box A and correct comparable forms eg $\frac{25}{60}$ and $\frac{24}{60}$ or $\frac{10}{24}$ and $\frac{10}{25}$ or $15:21$ and $14:21$ or $41.()\%$ or $42\%$ and $40\%$ or $0.41$ or $0.42$ and $0.4$ | Q1   | oe<br>Strand (ii) Logical argument with steps<br>shown         |  |  |
|    | Alternative method 2  |      |  |  |  |
|    | $\frac{2}{5} \times 12$ or 4.8<br>or $\frac{5}{12} \times 5$ or 2.08 or 2.1   | M1   | ое   |  |  |
|    | Box A and 4.8 (and 5)<br>or<br>Box A and 2.08 or 2.1 (and 2)  | Q1   | oe<br>Strand (ii) Logical argument with steps<br>shown         |  |  |